

Semester 2 Notes: Week 10 - Week 17 (03/15/21 - 05/07/21)

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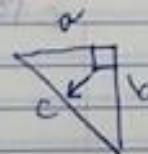
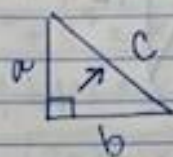
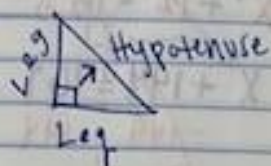
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Lesson One

The Pythagorean Theorem

- I can use the pythagorean theorem to find the missing length of a \triangle .



- * The hypotenuse is always side c *

The pythagorean theorem : $a^2 + b^2 = c^2$

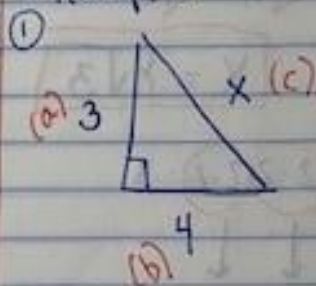
Exponent Review

$$X^2 = X \cdot X$$

$$4^2 = 4 \cdot 4 = 16$$

$$-6^2 = -6 \cdot -6 = 36$$

Examples



Find x

$2\sqrt{x}$

$$a^2 + b^2 = c^2$$

$$3^2 + 4^2 = x^2$$

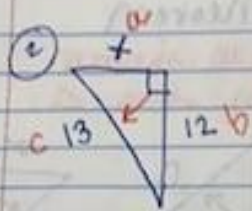
$$9 + 16 = x^2$$

$$\sqrt{25} = \sqrt{x^2}$$

$$\boxed{5 = x}$$

* opposite of x^2
is \sqrt{x} *

$$a^2 + b^2 = c^2$$



Find x

$$a^2 + b^2 = c^2$$

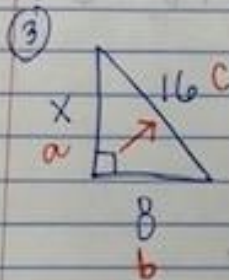
$$x^2 + 12^2 = 13^2$$

$$x^2 + 144 = 169$$

$$-144 \quad -144$$

$$x^2 = 25$$

$$x = 5$$



Find x

$$a^2 + b^2 = c^2$$

$$x^2 + 8^2 = 16^2$$

$$x^2 + 64 = 256$$

$$-64 \quad -64$$

$$x^2 = 192$$

$$x = 8\sqrt{3}$$

$$\sqrt{192}$$

$$\sqrt{64 \cdot 3}$$

$$8\sqrt{3}$$

$$13.546$$

$$(2 \cdot 2)(2 \cdot 2)(2 \cdot 2) \cdot 3$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$2 \cdot 2 \cdot 2 \sqrt{3}$$

$$8\sqrt{3}$$

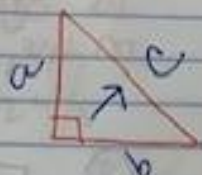
Lesson Two

04/27/2021 Pythagorean Theorem w/ Radicals
• I can use the Pythagorean theorem to solve for missing lengths.

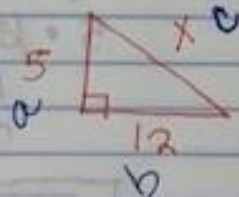
Warm-up

① What is the Pythagorean theorem?
 $a^2 + b^2 = c^2$

② Label this right triangle with sides a , b , and c .



③ Find x



$$a^2 + b^2 = c^2$$

$$5^2 + 12^2 = x^2$$

$$25 + 144 = x^2$$

$$\sqrt{169} = \sqrt{x^2}$$

$$13 = x$$

Radical Review

$$\begin{array}{c} \sqrt{45} \\ \wedge \\ 5 \cdot 9 \\ \wedge \\ 3 \cdot 3 \\ \downarrow \\ \boxed{3\sqrt{5}} \end{array}$$

① Find multiples

② Cross out the numbers you simplify.

③ circle any pairs.

④ write your pair as one number on the outside

Examples

$$\begin{array}{c} \textcircled{1} \sqrt{32} \\ \wedge \\ 4 \cdot 8 \\ \wedge \\ 2 \cdot 2 \quad \times \cdot 2 \\ \wedge \\ 2 \cdot 2 \\ \downarrow \quad \swarrow \\ 2 \cdot 2 \sqrt{2} \\ \boxed{4\sqrt{2}} \end{array}$$

$$\begin{array}{c} \textcircled{2} \sqrt{30} \\ \wedge \\ 5 \cdot 6 \\ \wedge \\ 2 \cdot 3 \\ \downarrow \\ \boxed{\sqrt{30}} \end{array}$$

4/28/21 Types of Triangles

• I can determine if a triangle is acute, right, or obtuse.

*Formulas:

$$a^2 + b^2 > c^2 \rightarrow \text{Acute } \Delta$$

$$a^2 + b^2 = c^2 \rightarrow \text{Right } \Delta$$

$$a^2 + b^2 < c^2 \rightarrow \text{Obtuse } \Delta$$

* C is always your longest side *

① 7, 8, 9
a b c

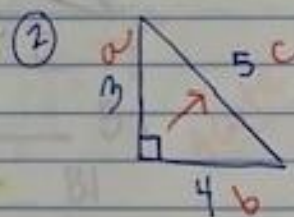
$$a^2 + b^2 \quad c^2$$

$$7^2 + 8^2 \quad 9^2$$

$$49 + 64 \quad 81$$



$$113 > 81 \text{ Acute}$$



$$a^2 + b^2 \quad c^2$$

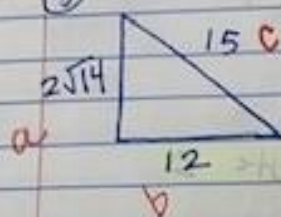
$$3^2 + 4^2 \quad 5^2$$

$$9 + 16 \quad 25$$

$$25 = 25$$

~~Right~~

#5 (3) Example



$$a^2 + b^2 = c^2$$

$$(\cancel{2\sqrt{14}})^2 + 12^2 = 15^2$$

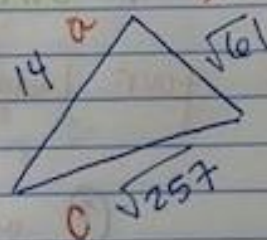
$$(2 \times 14) + 144 = 225$$

$$28 + 144 = 225$$

Obverse

$$172 < 225$$

#6 (4)



$$a^2 + b^2 = c^2$$

$$14^2 + \sqrt{61}^2 = \sqrt{257}^2$$

$$196 + 61 = 257$$

Right

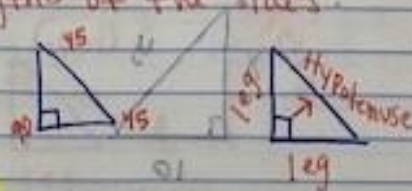
$$257 = 257$$

Lesson Four

5/3/21 Special Right Triangles

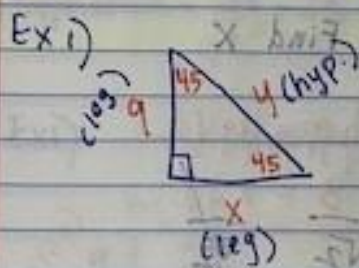
- I can use special right triangle rules to find lengths of the sides.

$$45^\circ - 45^\circ - 90^\circ$$



$$\text{leg} = \text{leg}$$

$$\text{Hypotenuse} = \text{leg} \cdot \sqrt{2}$$



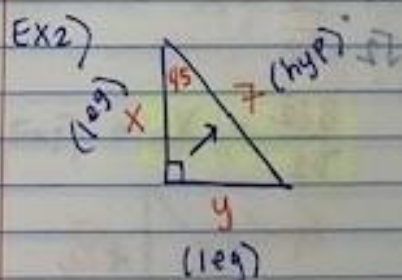
$$\text{leg} = \text{leg}$$

$$x = 9$$

$$\text{hyp} = \text{leg} \cdot \sqrt{2}$$

$$y = 9 \cdot \sqrt{2}$$

$$y = 9\sqrt{2}$$



$$\text{hyp} = \text{leg} \cdot \sqrt{2}$$

$$7 = x\sqrt{2}$$

$$\frac{7}{\sqrt{2}} = \frac{x\sqrt{2}}{\sqrt{2}}$$

$$\frac{7\sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} = x$$

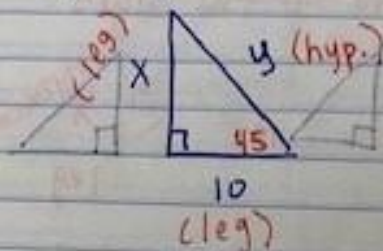
$$\text{leg} = \text{leg}$$

$$y = \frac{7\sqrt{2}}{2}$$

$$\frac{7\sqrt{2}}{2} = x$$

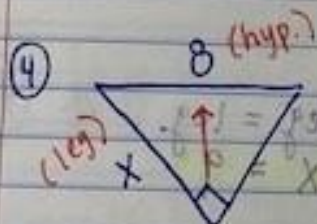
Special Right Triangles

③ leg = leg hyp = leg $\cdot \sqrt{2}$



leg = leg
hyp = 10

hyp = leg $\cdot \sqrt{2}$
y = 10√2



Find x

hyp = leg $\cdot \sqrt{2}$
8 = x√2
 $\frac{8}{\sqrt{2}} = \frac{x\sqrt{2}}{\sqrt{2}}$

√2 · $\frac{8}{\sqrt{2}}$ = x
8 = x

$\frac{8\sqrt{2}}{2} = x$

√2 · x = 8
√2 x = 8

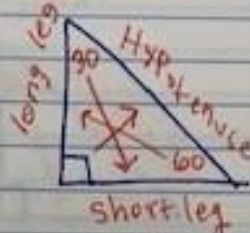
x = $\frac{8}{\sqrt{2}}$

x = $\frac{8\sqrt{2}}{2}$

8 = 8

05/04/21 Special Right Triangles Continued

- I can use special right Δ rules to find missing lengths.

 $30^\circ - 60^\circ - 90^\circ$


* Short leg: across from 30° .

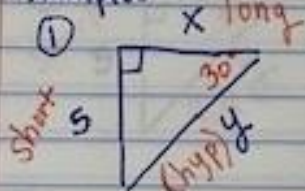
* Long leg: across from 60° .

Formulas:

$$\text{hyp} = \text{short leg} \cdot 2$$

$$\text{Long leg} = \text{short leg} \cdot \sqrt{3}$$

Examples:



$$\text{hyp} = \text{sh} \cdot 2$$

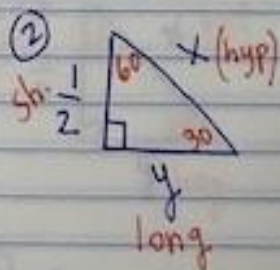
$$y = 5 \cdot 2$$

$$y = 10$$

$$\text{long} = \text{sh} \cdot \sqrt{3}$$

$$x = 5 \cdot \sqrt{3}$$

$$x = 5\sqrt{3}$$



$$\text{hyp} = \text{sh} \cdot 2$$

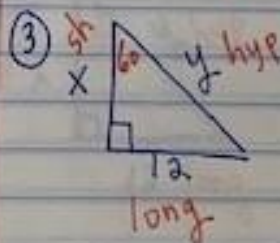
$$x = \frac{1}{2} \cdot 2$$

$$x = 1$$

$$\text{long} = \text{sh} \cdot \sqrt{3}$$

$$y = \frac{1}{2} \cdot \sqrt{3}$$

$$y = \frac{\sqrt{3}}{2}$$



$$\text{hyp} = \text{sh} \cdot 2$$

$$y = 2x$$

$$y = \frac{12\sqrt{3}}{3} \cdot \frac{2}{1}$$

$$y = \frac{24\sqrt{3}}{3}$$

$$\text{long} = \text{sh} \cdot \sqrt{3}$$

$$\sqrt{3} \cdot \frac{12}{\sqrt{3}} = \frac{x\sqrt{3}}{\sqrt{3}}$$

$$\frac{12\sqrt{3}}{3} = x$$